MATH 54 SUMMER 2017, QUIZ 29

Suppose A is a 2×2 matrix and that $\mathbf{v}_1$ is an eigenvector of A with eigenvalue 2 and $\mathbf{v}_2$ is an eigenvector of A with eigenvalue -2.

$$\mathbf{v}_1 = \begin{bmatrix} 2 \\ 1 \end{bmatrix} \quad \mathbf{v}_2 = \begin{bmatrix} 1 \\ 3 \end{bmatrix}$$

(a) Find the general solution to $\mathbf{y}' = A\mathbf{y}$

(b) Draw a picture of all solutions to $\mathbf{y}' = A\mathbf{y}$. Make sure to include the solutions that always stay in some eigenspace of A.