- 1. Confidence intervals versus hypothesis tests. Suppose we gather data from an unknown distribution which we can assume to be normal. If we have  $n = 10\ 000$ ,  $\bar{X} = 100$  and  $s^2 = 4$ , then
  - (a) Find a 99% confidence interval for  $\mu$ .
  - (b) Find a 99% one-sided confidence interval for an upper bound for  $\mu$ .

For what values of  $\mu_0$  would we reject (at 99%) the null hypothesis  $\mu = \mu_0$ 

- (c) with the alternate hypothesis  $\mu \neq \mu_0$ ?
- (d) with the alternate hypothesis  $\mu > \mu_0$ ?

This provides another interpretation of confidence intervals.

Here's a partial z-table for your use

$\alpha$	0.050	0.025	0.020	0.010	0.005	0.001
$z_{\alpha}$	1.645	1.960	2.054	2.326	2.576	3.090

- 2. Understanding confidence intervals. Suppose we're using a confidence interval to estimate a mean. What happens to the interval if
  - (a) Our confidence level increases?
  - (b) n increases, assuming everything else is constant?
  - (c)  $s^2$  increases, assuming everything else is constant?
  - (d)  $\bar{X}$  increases, assuming everything else is constant?
  - (e) we scale all the data by a constant multiple?